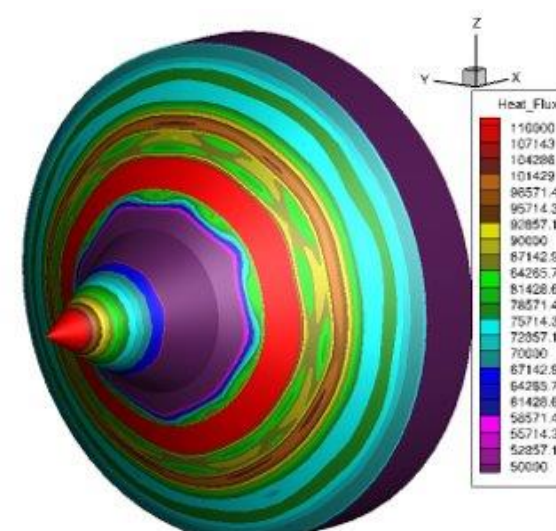




Characterization of Hypersonic Instabilities over a Double Cone



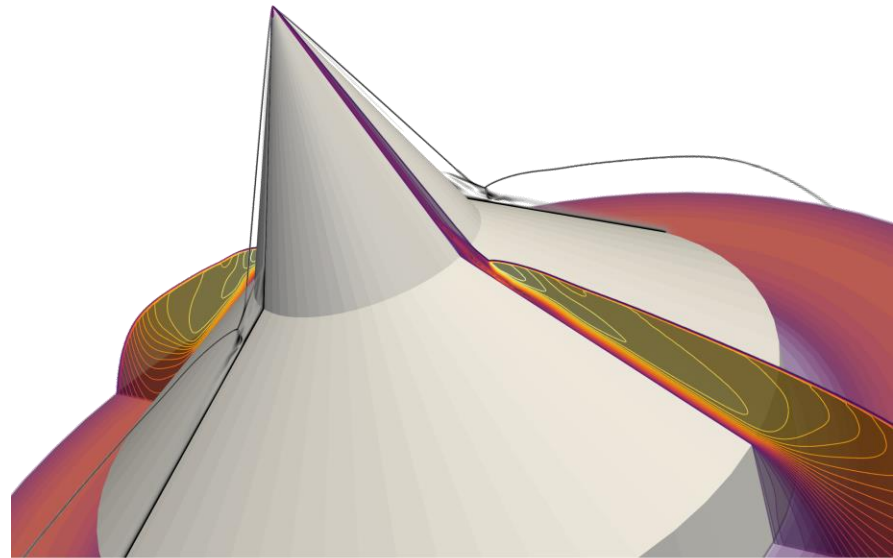
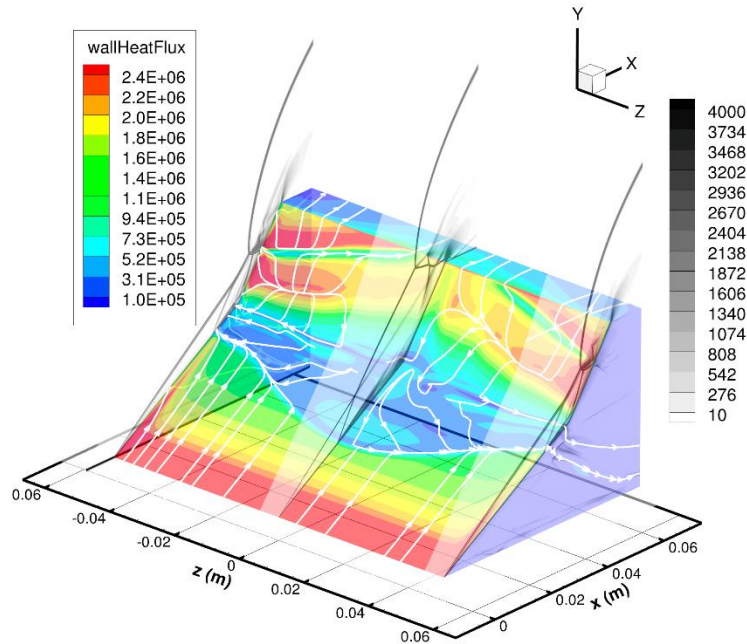
Ozgur Tumuklu and Kyle M. Hanquist

Rensselaer Polytechnic Institute

The University of Arizona

AIAA Paper 2024-1481

Background



This work briefly aims to:

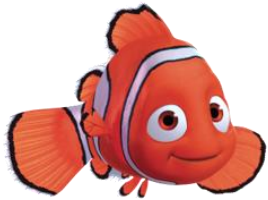
- investigate the **instabilities** resulted from complex shock wave boundary layer interactions (SWBLIs) over double wedges and double cones.
- compare findings with measured data and high-fidelity previous DSMC simulations.
- estimate **temporal characteristics** of flows to provide data to experimentalists using 2-D and full 3-D configurations.
- characterize the 3D instabilities with different Reynolds numbers.
- An open-source frameworks*,** were used to model SWBLIs.

*Casseau, V., Palharini, R.C., Scanlon, T.J., and Brown, R.E., "A two-temperature open-source CFD model for hypersonic reacting flows, part one: zero-dimensional analysis," *Aerospace*, Vol. 3, No. 4, 2016, p. 34.

** Maier, et al., "Development of Physical and Numerical Nonequilibrium Modeling Capabilities within the SU2-NEMO Code," AIAA Paper 2023-3488.

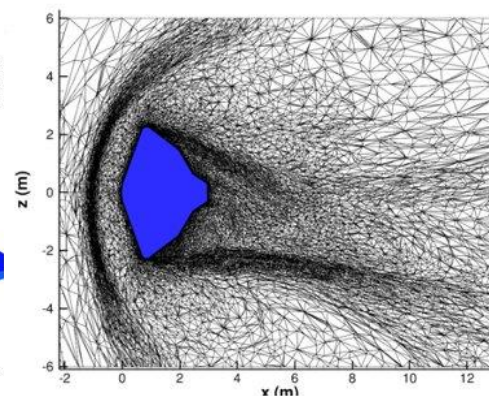
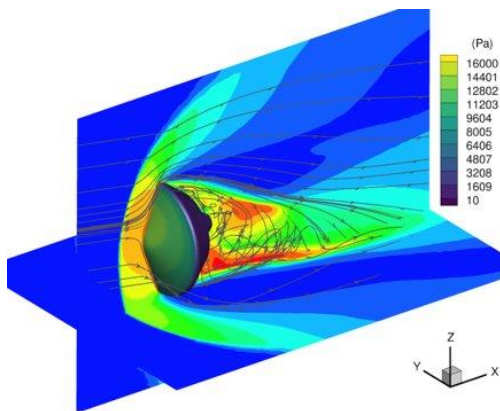
SU2-NonEquilibriumMOdels (NEMO)*

- Extension of SU2 for nonequilibrium, high-temperature, and high-speed flows,
- Continuum/slip regime, steady, viscous, multi-component, gas mixtures in thermochemical nonequilibrium,
- Finite-rate chemistry and thermal nonequilibrium,
- Catalytic wall, slip BC, and radiative equilibrium BC,
- Inherits, a lot of strengths from SU2 (design, multi-physics),
- Convective fluxes with MUSCL and limiting on primitives (MSW, AUSM, AUSM+up2).



$$\frac{\partial \mathbf{U}}{\partial t} + \nabla \cdot \mathbf{F}^c(\mathbf{U}) - \nabla \cdot \mathbf{F}^v(\mathbf{U}, \nabla \mathbf{U}) - \mathbf{Q}(\mathbf{U}) = 0$$

$$\mathbf{U} = \begin{pmatrix} \rho_1 \\ \vdots \\ \rho_{n_s} \\ \rho \mathbf{u} \\ \rho e \\ \rho e^{ve} \end{pmatrix}, \quad \mathbf{F}^c = \begin{pmatrix} \rho_1 \mathbf{u} \\ \vdots \\ \rho_{n_s} \mathbf{u} \\ \rho \mathbf{u} \mathbf{u}^T + P \mathbf{I} \\ \rho h \mathbf{u} \\ \rho e^{ve} \mathbf{u} \end{pmatrix}, \quad \mathbf{F}^v = \begin{pmatrix} -J_1 \\ \vdots \\ -J_{n_s} \\ \sigma \\ \mathbf{u}^T \sigma - \sum_k \mathbf{q}^k - \sum_s J_s h_s \\ -\mathbf{q}^{ve} - \sum_s J_s e_s^{ve} \end{pmatrix}, \quad \mathbf{Q} = \begin{pmatrix} \dot{\omega}_1 \\ \vdots \\ \dot{\omega}_{n_s} \\ \mathbf{0} \\ 0 \\ \dot{\Theta}^{tr:ve} + \sum_s \dot{\omega}_s e_s^{ve} \end{pmatrix}$$

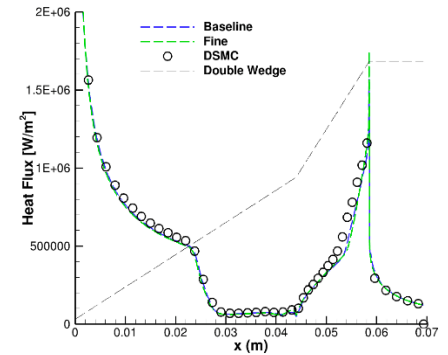
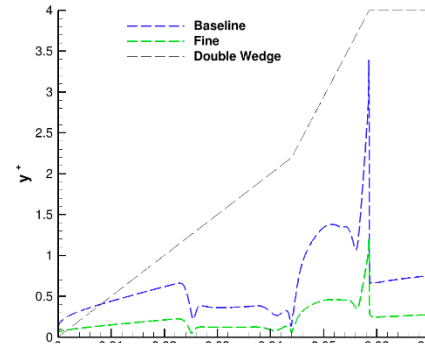
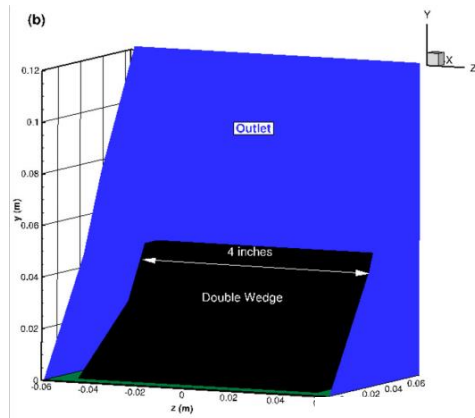


<https://github.com/su2code/SU2.git>

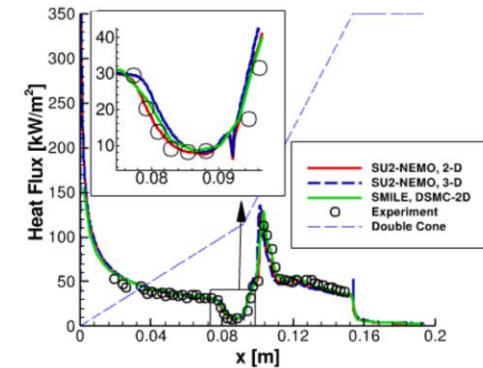
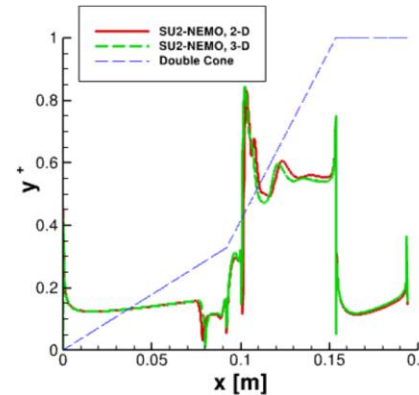
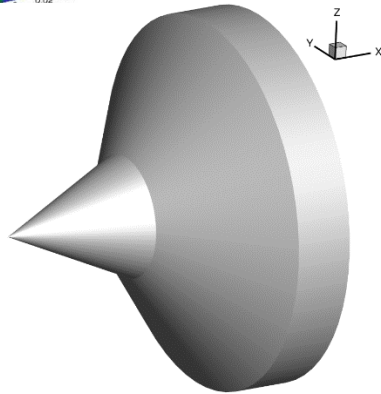
*Maier, et al., "Development of Physical and Numerical Nonequilibrium Modeling Capabilities within the SU2-NEMO Code," AIAA Paper 2023-3488.

Grid Convergence

Double Wedge*



Double Cone

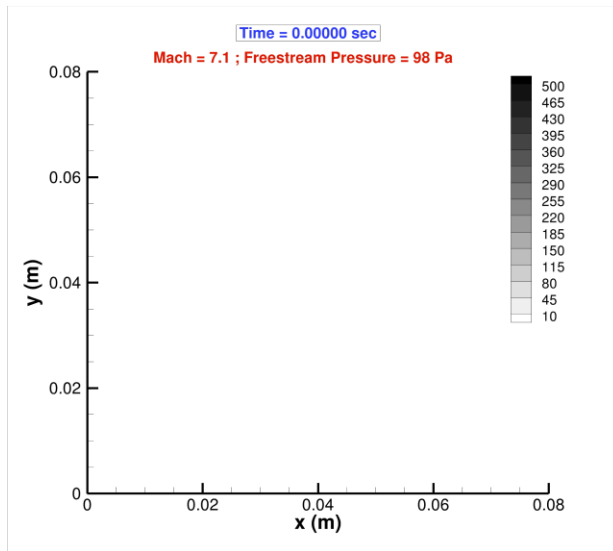


- Structured meshes with two different number of grids are used.
- Rigorous grid study is carried out to ensure that the results are independent of grid resolutions
- 71,000 surface elements along with about **28M grids** were used for the double cone cases whereas 50M grids were used for 3D double wedge calculations.

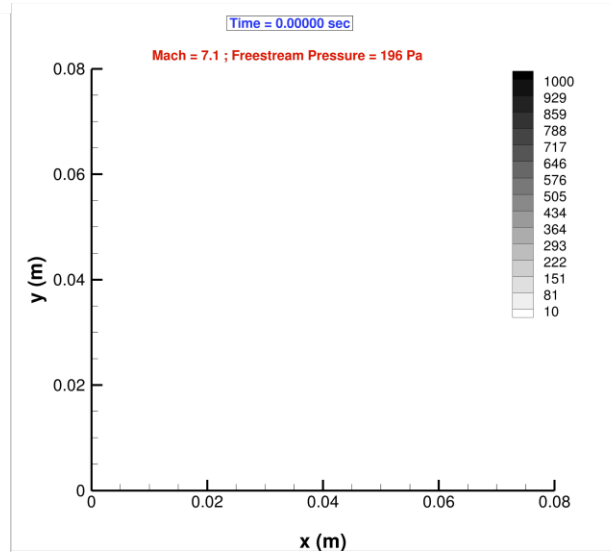
Temporal Characteristics of Shock Structure

2D Double Wedge*

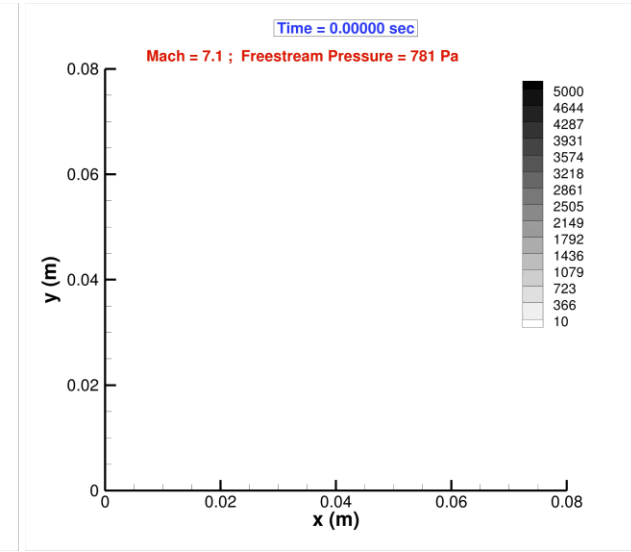
P = 98 Pa



P = 196 Pa



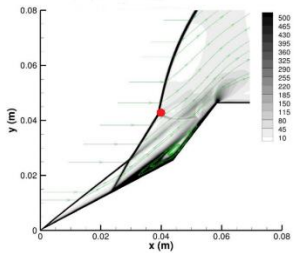
P = 781 Pa



- The lowest pressure case reaches steady state at about 0.75 ms
- Periodic oscillations seen in the medium pressure (P=196 Pa) case.
- The oscillations disappear for the highest-pressure case but flow reaches steady state about 2 ms (**10X times** larger than the duration of the experiment).

*Tumuklu, O., & Hanquist, K. M. (2023). Unsteadiness of hypersonic flows over a double wedge. In *AIAA SCITECH 2023 Forum* (p. 0860).

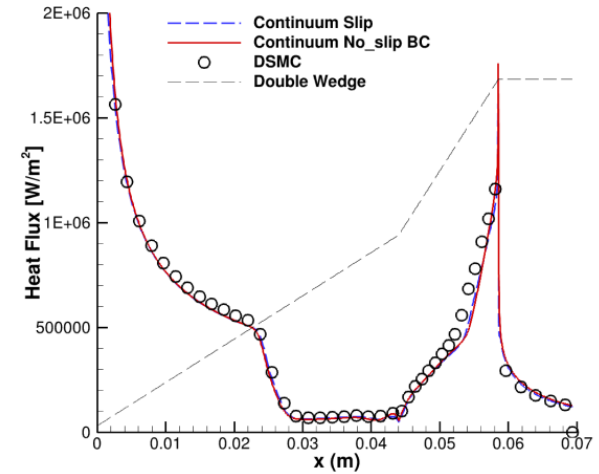
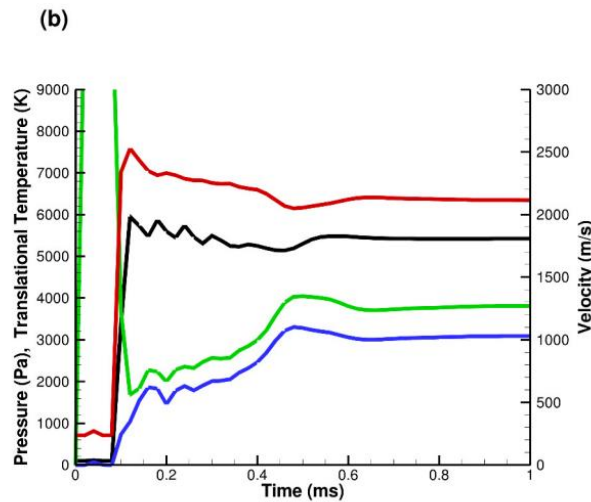
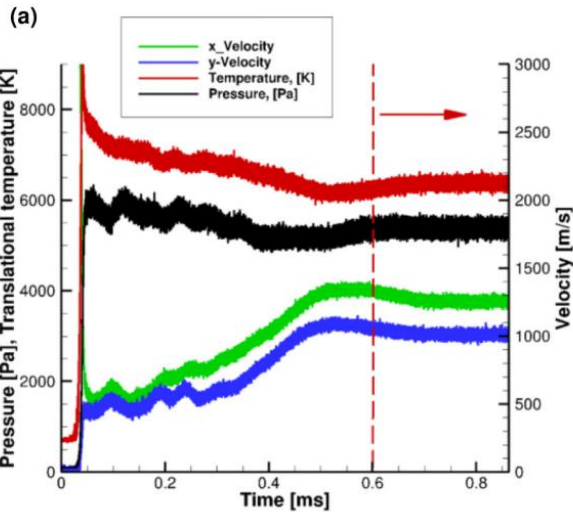
Accuracy Current Continuum Simulations over Double Wedge



2D, DSMC, 98 Pa*

2D, NS, 98 Pa**

Rarefied effects**



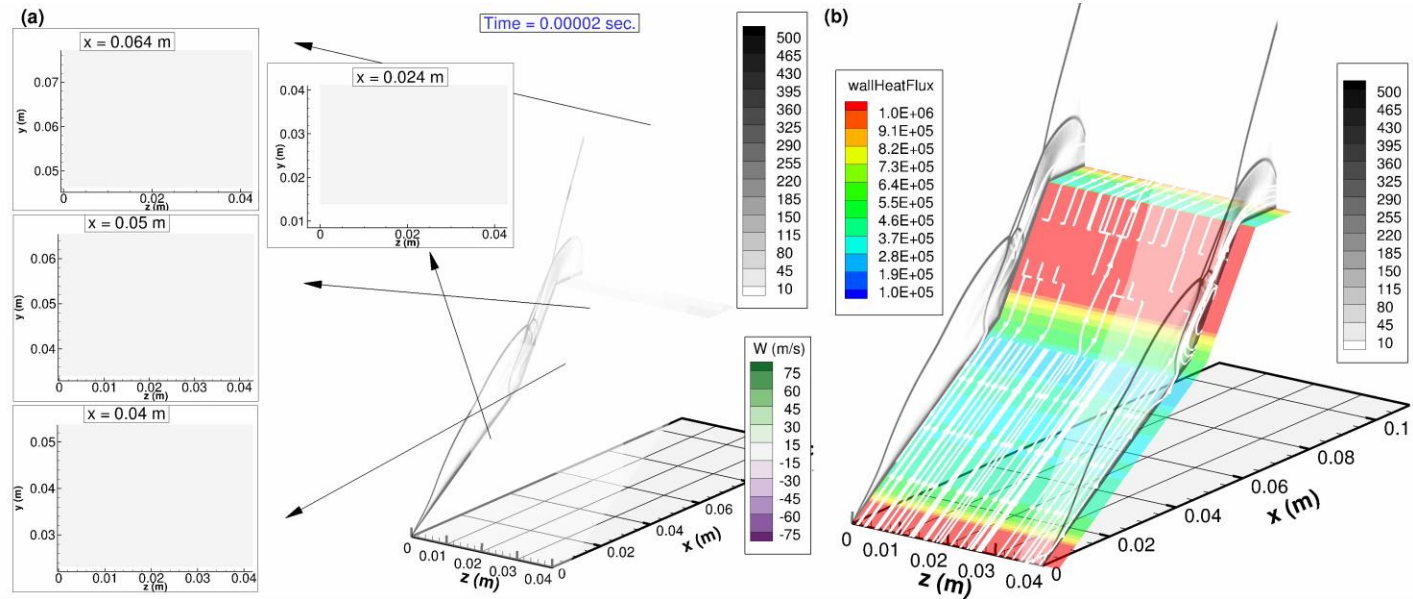
- The temporal evolutions are found to be **the same** for DSMC and NS.
- The impact of rarefied effects, even for **the lowest Re**, is negligible.

*Tumuklu, O., Levin, D. A., and Theofilis, V., "On the temporal evolution in laminar separated boundary layer shock-interaction flows using DSMC," AIAA Paper 2017-1614, 2017.

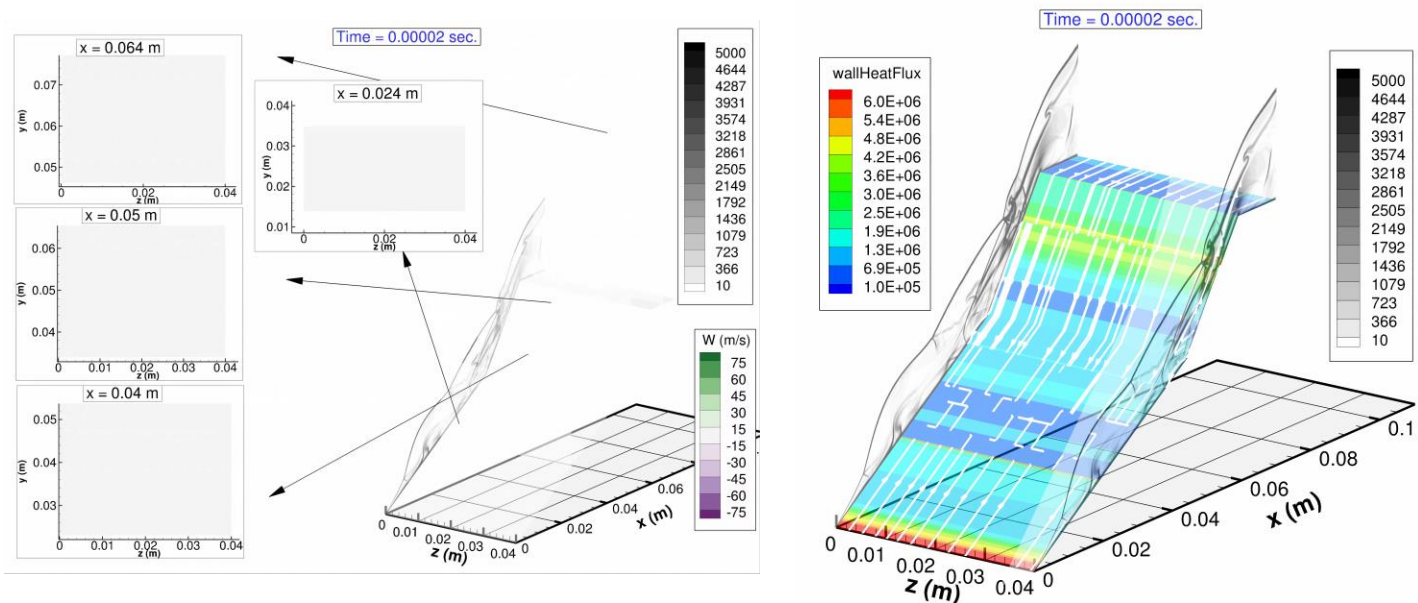
**Tumuklu, O., and Hanquist, K. M., "Temporal characteristics of hypersonic flows over a double wedge with Reynolds number," Physics of Fluids, Vol. 35, No. 10, 2023.

Periodic 3-D Simulations over Double Wedge

P = 98 Pa

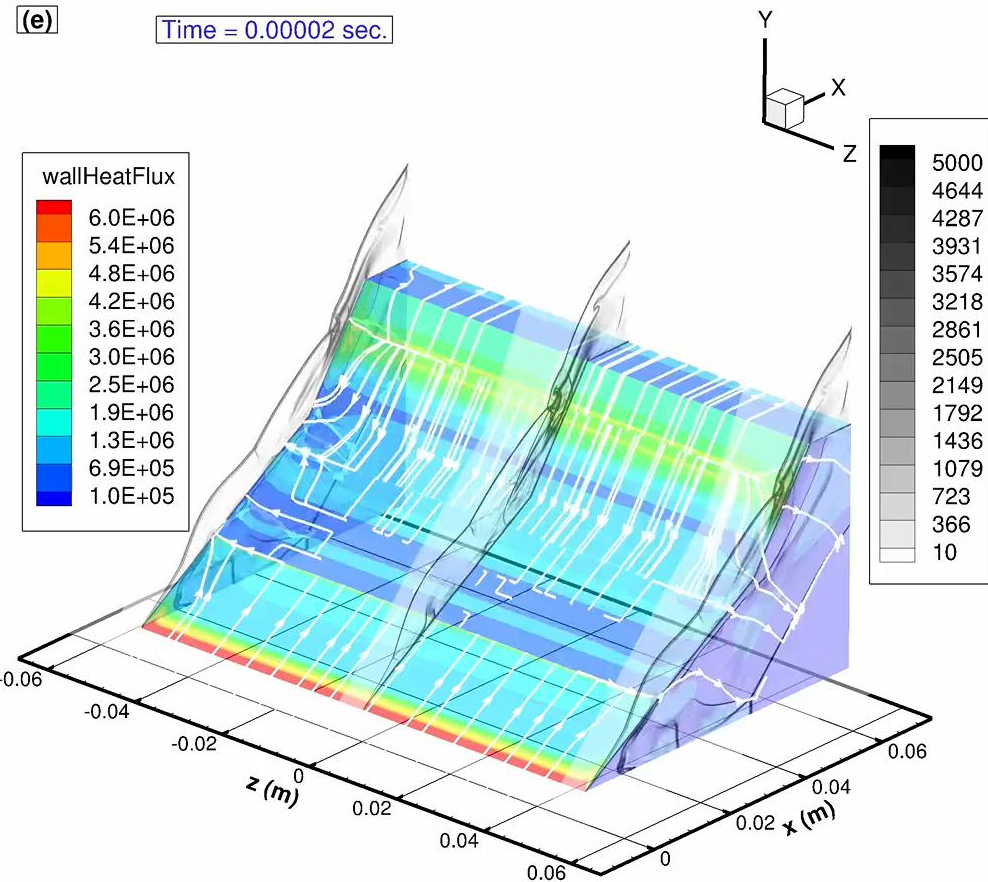
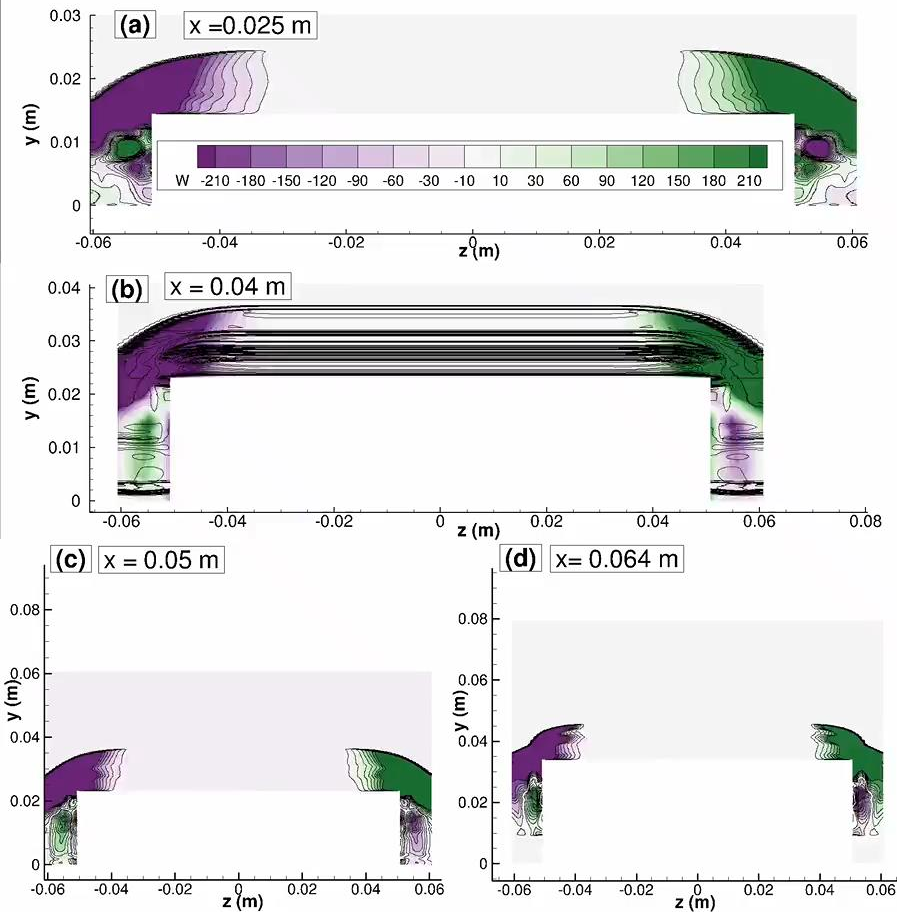


P = 781 Pa



Full 3D Simulations over Double Wedge*

$P = 781 \text{ Pa}$

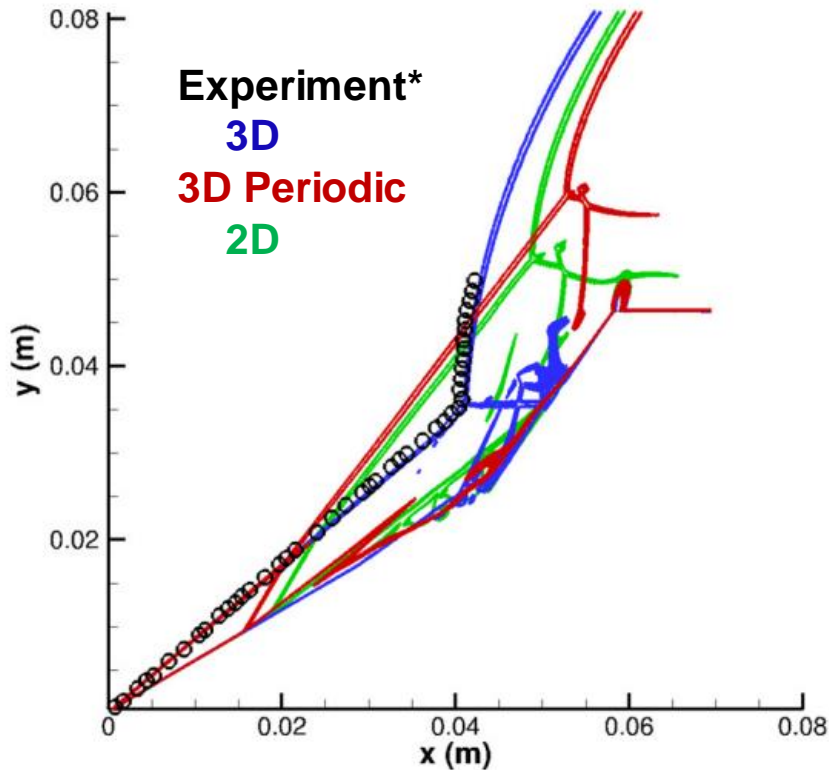


- The structure of the spanwise instabilities close to the center is found to be very similar to 3D periodic cases.

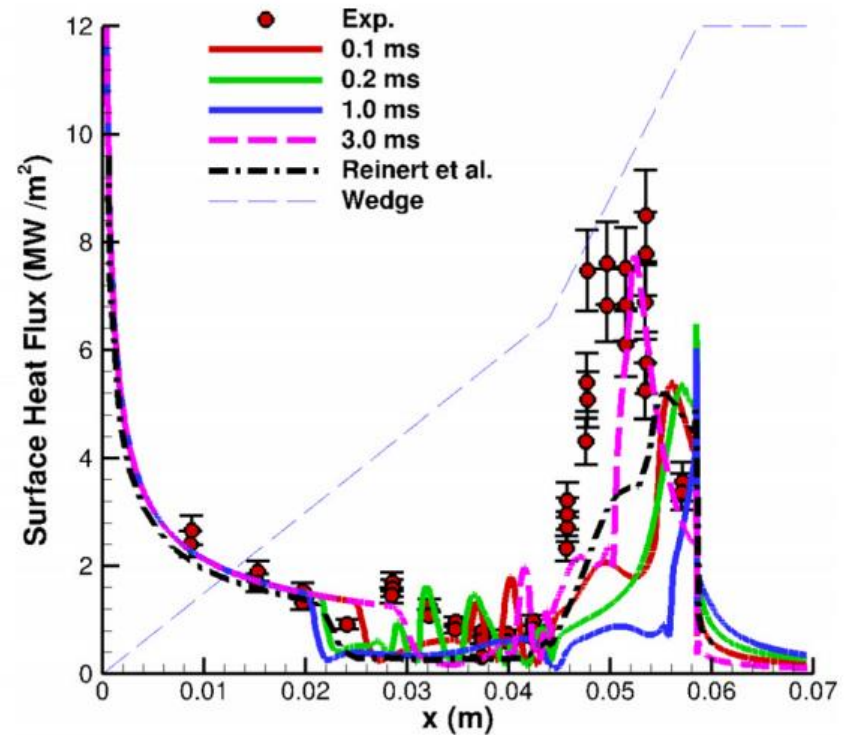
*Tumuklu, O., and Hanquist, K. M., "Temporal characteristics of hypersonic flows over a double wedge with Reynolds number," Physics of Fluids, Vol. 35, No. 10, 2023.

Effect of Geometric Configurations*

Shock Structures



Surface Heating



- Good agreement is achieved between the full 3D calculations and experiments.

*Tumuklu, O., and Hanquist, K. M., "Temporal characteristics of hypersonic flows over a double wedge with Reynolds number," *Physics of Fluids*, Vol. 35, No. 10, 2023.

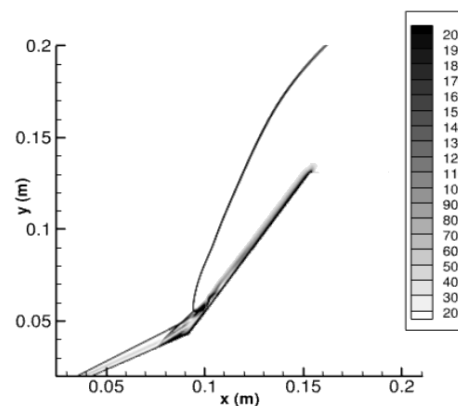
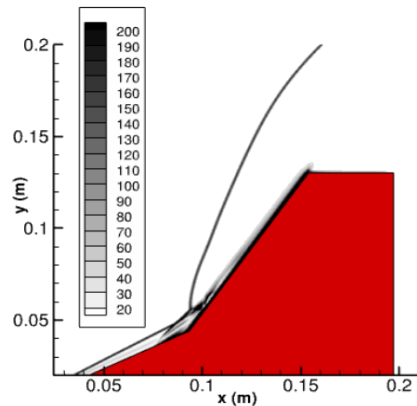
Reinert, J. D., Candler, G. V., and Komives, J. R., "Simulations of unsteady three-dimensional hypersonic double-wedge flow experiments," *AIAA Journal*, Vol. 58, No. 9, 2020, pp. 4055–4067.

Comparison of Shock Structure with DSMC over Double Cone

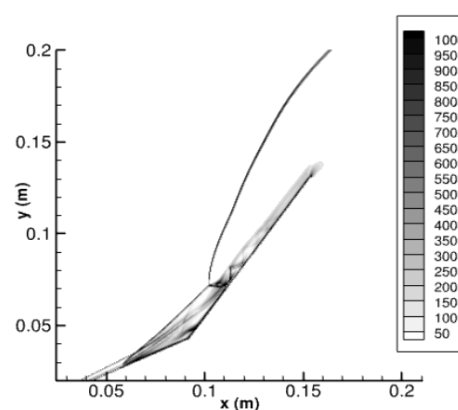
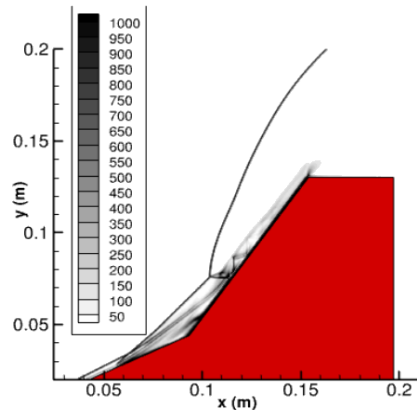
Kinetic Approach DSMC*

Continuum Approach

P = 2.2 Pa



P = 8.8 Pa

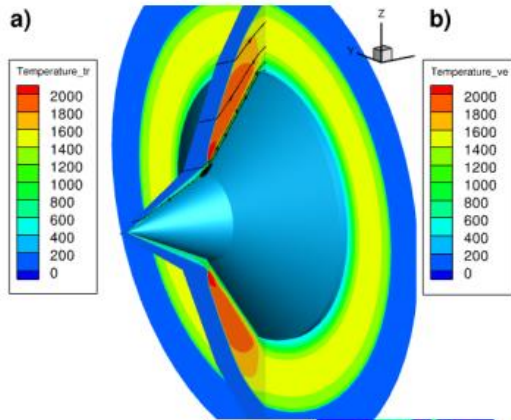


- Excellent agreement is achieved with the previous DSMC work*.
- The reflection of the compression and expansion waves through the shear layer is captured accurately.

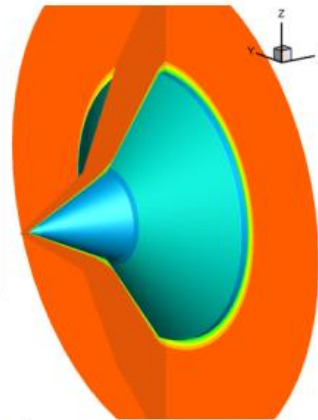
* Tumuklu, O., Levin, D. A., and Theofilis, V., "Investigation of unsteady, hypersonic, laminar separated flows over a double cone geometry using a kinetic approach," Physics of Fluids, Vol. 30, No. 4, 2018, p. 046103.

3-D Effects on the Flowfield for $P_\infty = 2.2 \text{ Pa}$

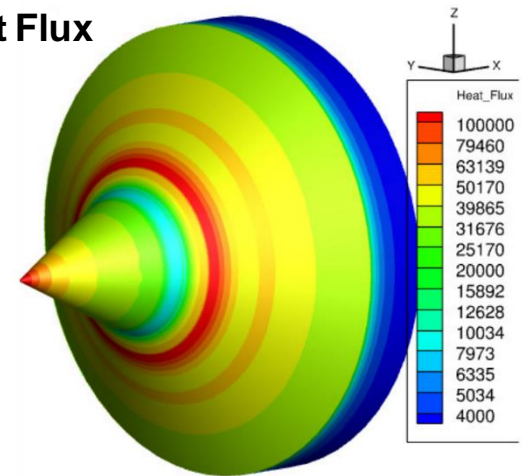
Ttrn



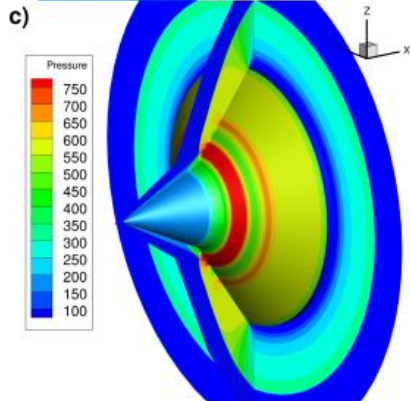
Tvib



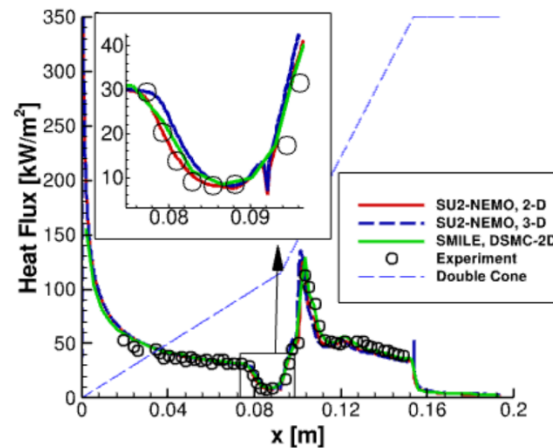
Heat Flux



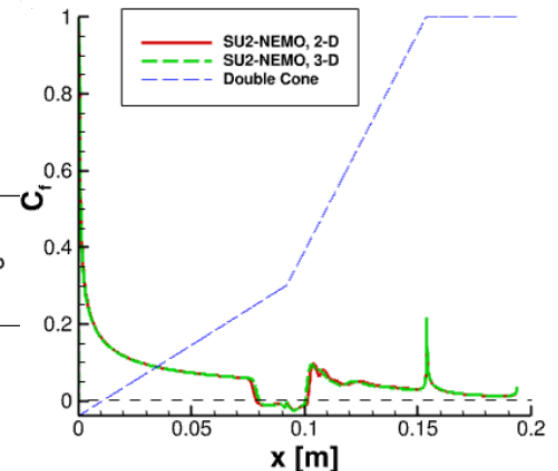
Pressure



Heat Flux

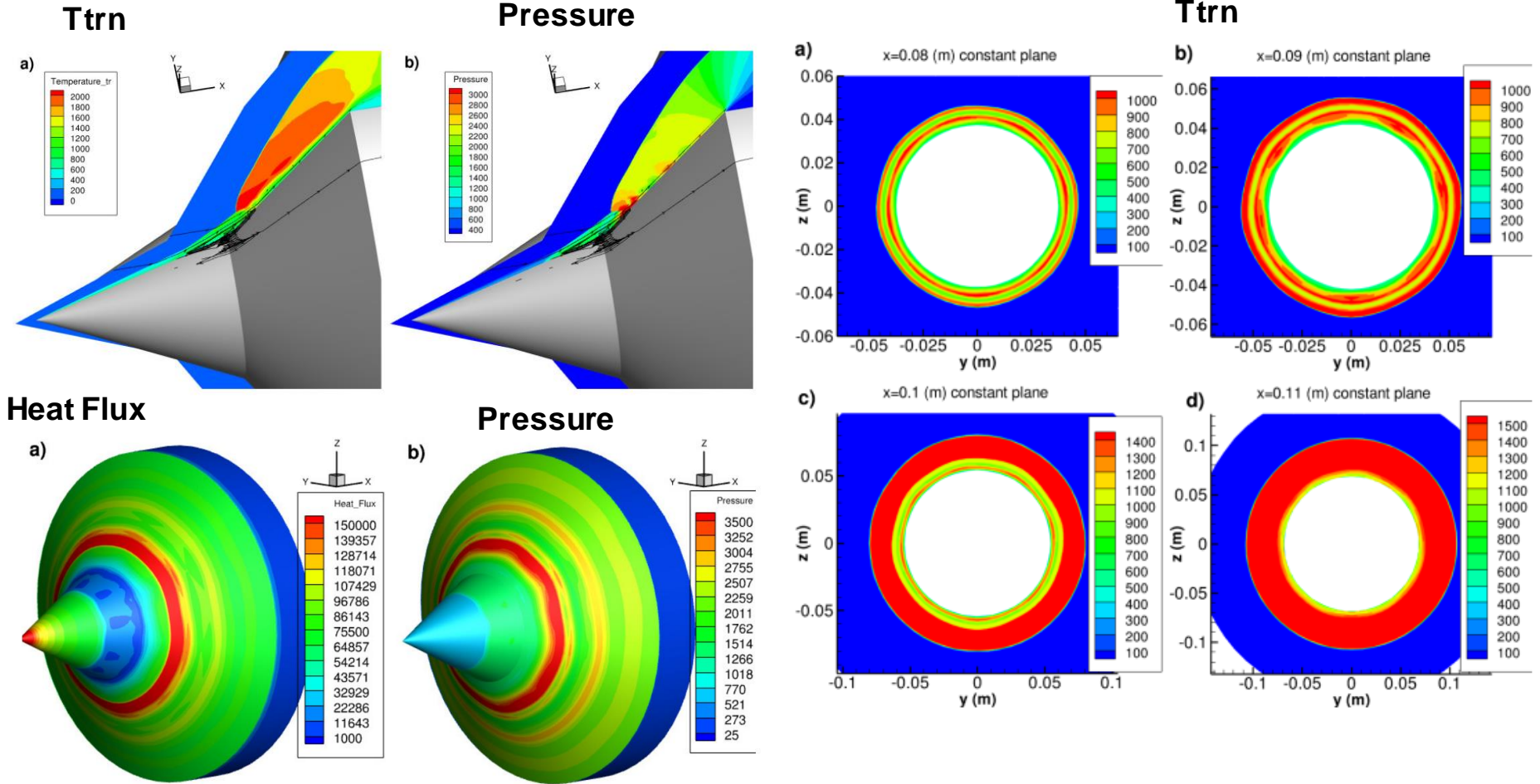


Skin Friction Coeff.



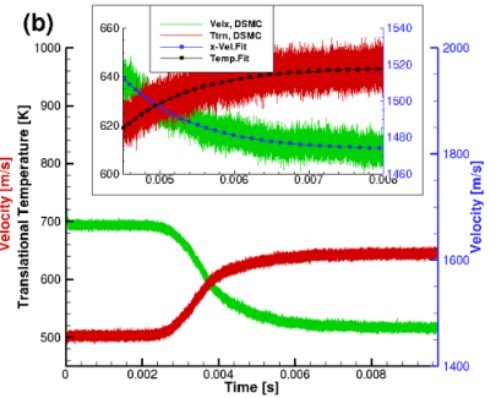
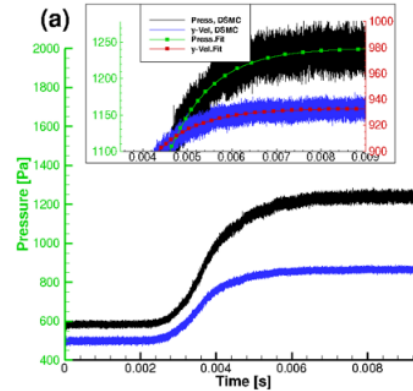
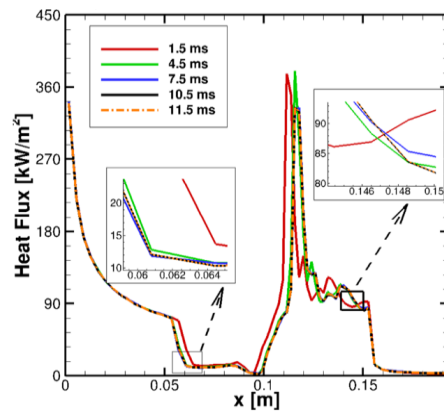
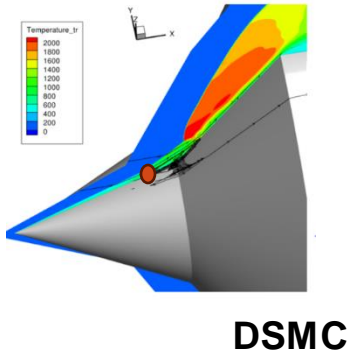
- Excellent agreement is achieved with 2-D and full 3-D calculations, indicating that **the absence of spanwise instabilities**.

3-D Effects on the Flow for $P_\infty = 8.8 \text{ Pa}$

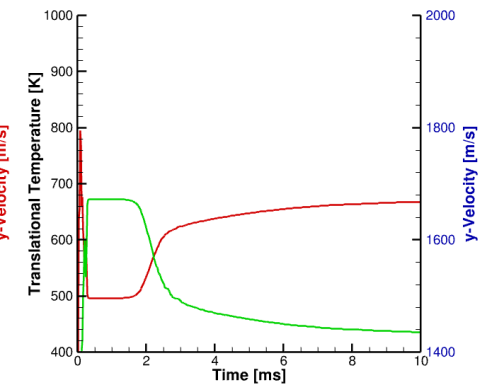
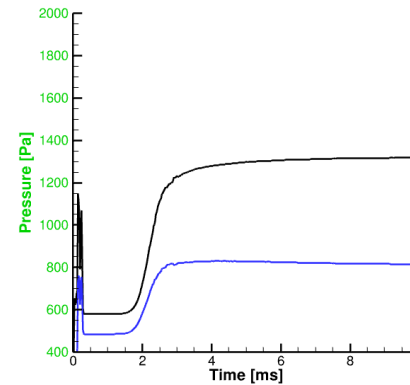
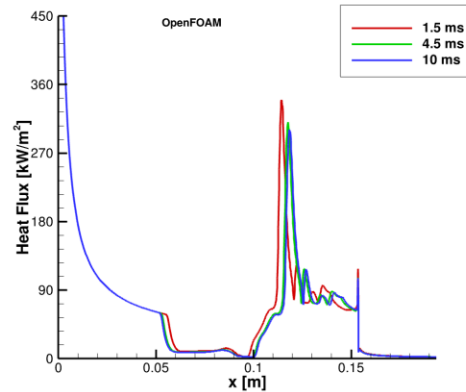


- The onset of 3-D instabilities is reported for the high Re case.

Temporal Comparison of the Surface and Flow Fields for Double Cone



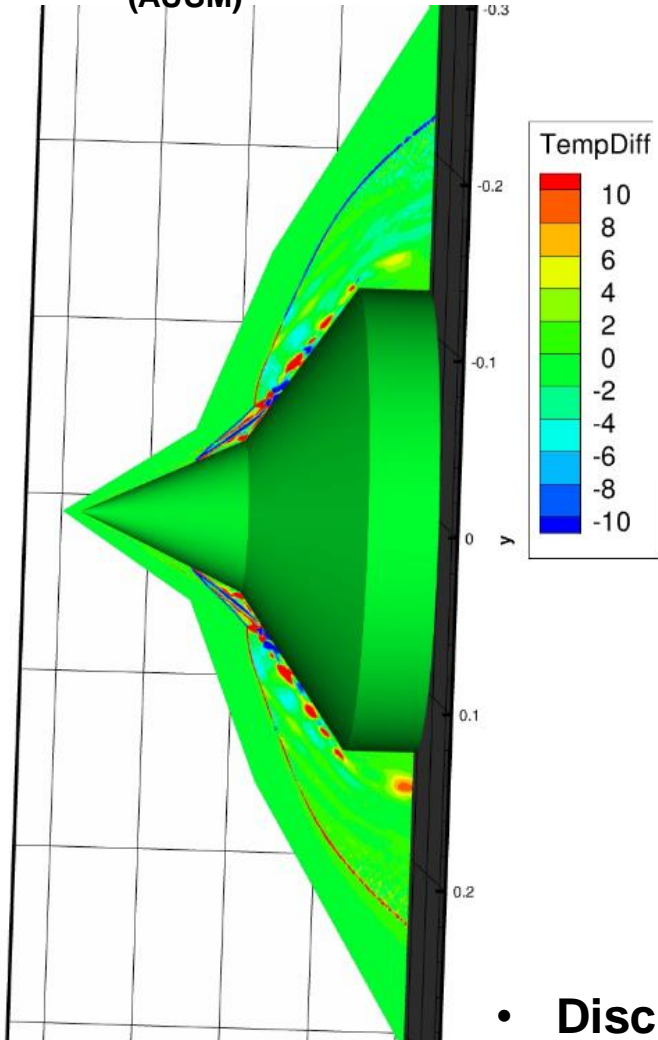
NS



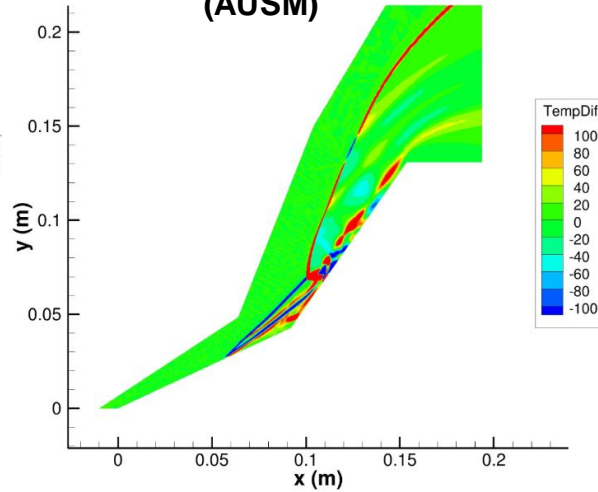
- **Temporal characteristics** of both kinetic and continuum solvers are compared, and very good agreement is achieved.
- Slight differences are seen in the temporal evolutions, but the decay rates are consistent with the previous DSMC data.

Characterization of KH instability on the Flow Field

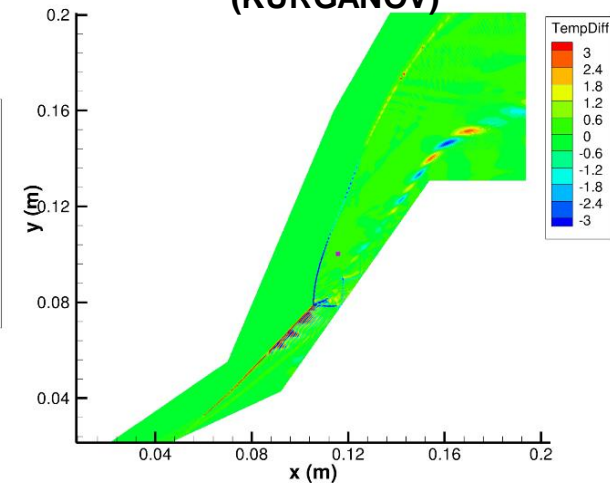
3-D, SU2-NEMO
(AUSM)



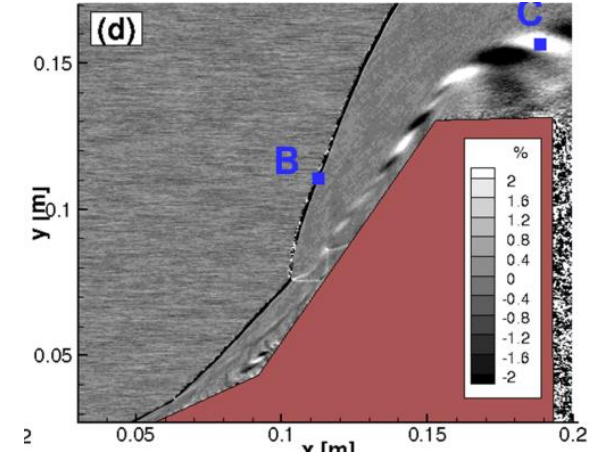
2-D, SU2-NEMO
(AUSM)



2-D, HY2FOAM
(KURGANOV)



2-D, DSMC*

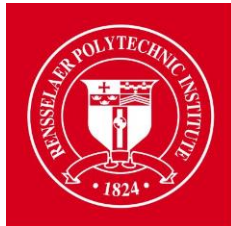


- **Discrepancies** are observed when employing different convective schemes.

* Tumuklu, O., Levin, D. A., and Theofilis, V., "Investigation of unsteady, hypersonic, laminar separated flows over a double cone geometry using a kinetic approach," Physics of Fluids, Vol. 30, No. 4, 2018, p. 046103.

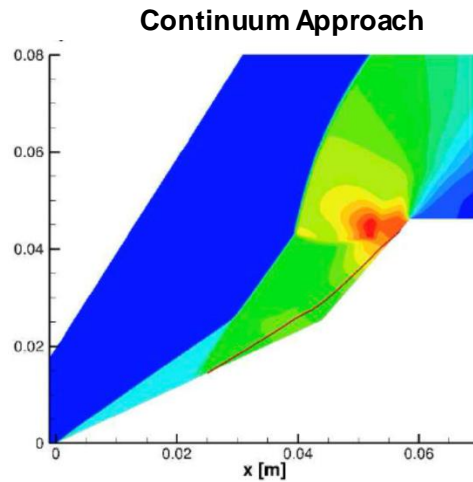
Conclusions

- Rigorous comparisons were made previous DSMC work, excellent agreement was achieved.
- Ongoing efforts focus on the **characteristics of 3-D instabilities** at different Re and wedge/cone angles.
- The implementation of **WMLES** using GPUs is under consideration to study a wide spectrum of **Re** .
- The effect of the real gas effects using **Mutation++** is under consideration.
- The impact of the surface temperature on the structure of the spanwise instabilities will be investigated.

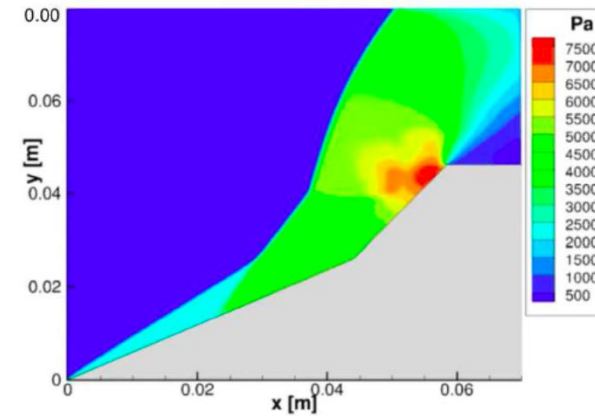


Comparison of Pressure Field with DSMC

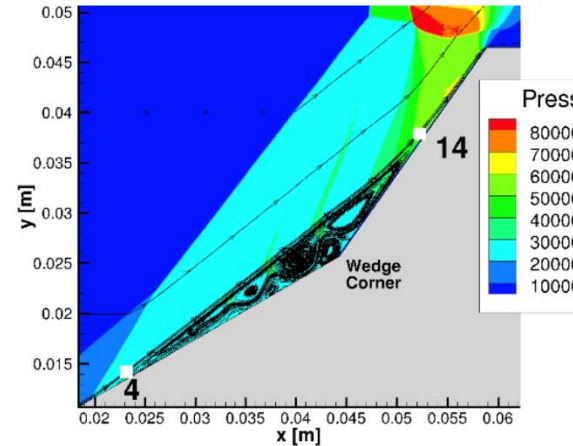
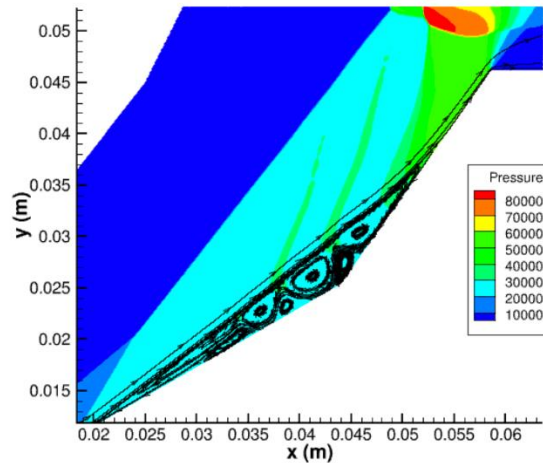
$P = 98 \text{ Pa}$



Kinetic Approach DSMC*



$P = 781 \text{ Pa}$



- Excellent agreement is achieved with the previous DSMC work.

*Tumuklu, O., Levin, D.A., and Theofilis V., On the temporal evolution in laminar separated boundary layers shock-interaction flows using DSMC, *55th AIAA Aerospace Sciences Meeting*, 2017, p. 1614